

LARGE-SAMPLE z -TEST ABOUT POP. PROPORTION p [DEVORE 8.4]

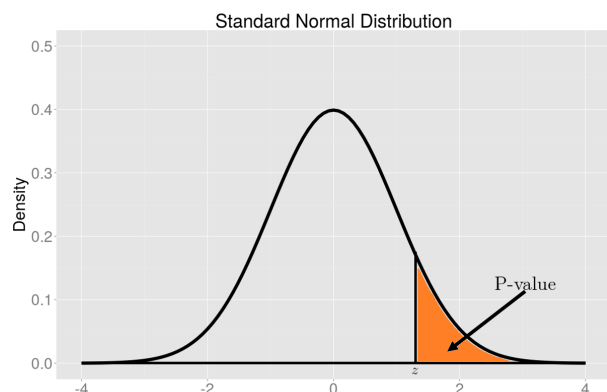
• LARGE-SAMPLE z -TEST ABOUT POPULATION PROPORTION p (SUMMARY):

Population:	Unknown proportion p of "successes"	
Random Sample:	$\mathbf{X} := (X_1, X_2, \dots, X_n)$	
Realized Sample:	$\mathbf{x} := (x_1, x_2, \dots, x_n)$	
Test Statistic	$W(\mathbf{X}; p_0)$	$Z = \frac{(X/n) - p_0}{\sqrt{p_0 q_0/n}}$
Test Statistic Value	$W(\mathbf{x}; p_0)$	$z = \frac{\hat{p} - p_0}{\sqrt{p_0 q_0/n}}$
$\hat{p} := x/n, q_0 := 1 - p_0, \min\{np_0, nq_0\} \geq 10$		
$x \equiv \#$ "Successes" in realized sample \mathbf{x}		

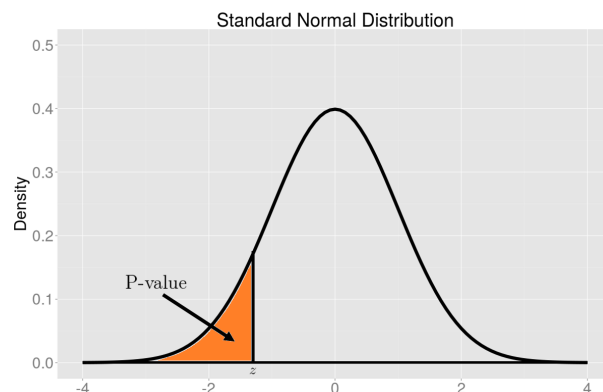
HYPOTHESIS TEST:	P-VALUE DETERMINATION:
$H_0 : p = p_0$ vs. $H_A : p > p_0$	P-value = $\mathbb{P}(Z \geq z) = 1 - \Phi(z)$
$H_0 : p = p_0$ vs. $H_A : p < p_0$	P-value = $\mathbb{P}(Z \leq z) = \Phi(z)$
$H_0 : p = p_0$ vs. $H_A : p \neq p_0$	P-value = $\mathbb{P}(Z \geq z) = 2 \cdot [1 - \Phi(z)]$

Decision Rule: If P-value $\leq \alpha$ then reject H_0 in favor of H_A
 If P-value $> \alpha$ then accept H_0 (i.e. fail to reject H_0)

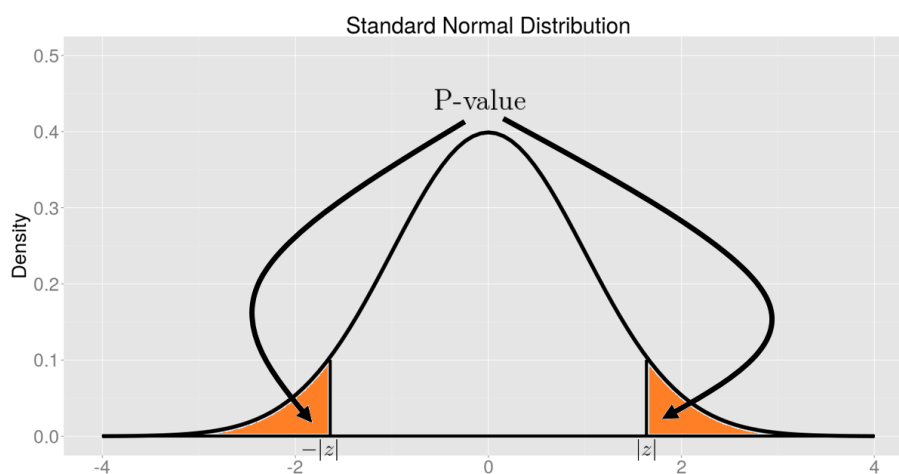
• LARGE-SAMPLE z -TEST ABOUT POPULATION PROPORTION p (P-VALUES VISUALIZED):



$H_0 : p = p_0$
 $H_A : p > p_0$



$H_0 : p = p_0$
 $H_A : p < p_0$



$H_0 : p = p_0$
 $H_A : p \neq p_0$

EX 8.4.1:

A long-time dollar store owner determined 10 years ago that 38% of customers paid with a credit card.

Recently, he looked backed at the payment methods of 80 customers from last quarter's records.

He discovered that 51 of those customers purchased with a credit card.

Does the sample data suggest that more customers are paying with a credit card these days??

(Use significance level $\alpha = 0.01$)

- (a) State the appropriate null hypothesis H_0 & alternative hypothesis H_A .
- (b) Compute the appropriate test statistic value for this hypothesis test.
- (c) Compute the resulting P-value.
- (d) Make the appropriate decision.

EX 8.4.2:

A long-time dollar store owner determined 5 years ago that 21 out of 50 customers paid with a credit card.

Recently, he looked backed at the payment methods of 120 customers from last quarter's records.

He discovered that fifty-five of those customers purchased with a credit card.

Does the sample data suggest that the proportion of credit card paying customers has changed nowadays??

(Use significance level $\alpha = 0.05$)

- (a) State the appropriate null hypothesis H_0 & alternative hypothesis H_A .
- (b) Compute the appropriate test statistic value for this hypothesis test.
- (c) Compute the resulting P-value.
- (d) Make the appropriate decision.