

Visualizing Data: Freq. Tables, Histograms

Engineering Statistics
Section 1.2

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Descriptive Statistics

Recall that Statistics consists of two broad branches:

- Descriptive Statistics
- Statistical Inference

The remainder of this chapter focuses squarely on Descriptive Statistics:

Definition

Descriptive Statistics is the organization, summary, visualization and presentation of data that conveys useful information about the data.

Descriptive Statistics involves:

- Data Visualization (this section)
- Numerical Summaries (Sections 1.3 & 1.4)

Data Visualizations

The following data visualizations will never be considered in this course:

- Stem-and-Leaf Displays
- Bar Charts
- Pie Charts
- Control Charts
- Scatter Plots
- Dot Plots
- Line Plots
- Contour Plots
- Radar Plots
- Violin Plots
- Heatmaps

So which data visualizations will be considered in this course??

- Frequency Tables (this section)
- Histograms (this section)
- Boxplots (Section 1.4)
- Frequency Polygons (Chapter 3)

Frequency Tables

Given a sample of eye colors:

H, Br, Br, Br, S, A, H, H, G, A, Bl, Bl, Br, Bl, A, Br, H, G, A, A, Br, Bl, G, Bl, Bl

Then the resulting frequency table is:

| EYE COLOR | FREQUENCY | RELATIVE FREQUENCY |
|------------------|------------------|---------------------------|
| Amber (A) | | |
| Blue (Bl) | | |
| Brown (Br) | | |
| Green (G) | | |
| Hazel (H) | | |
| Silver (S) | | |
| TOTAL: | | |

Frequency Tables

Given a sample of eye colors:

H, Br, Br, Br, S, A, H, H, G, A, Bl, Bl, Br, Bl, A, Br, H, G, A, A, Br, Bl, G, Bl, Bl

Then the resulting frequency table is:

| EYE COLOR | FREQUENCY | RELATIVE FREQUENCY |
|------------------|------------------|---------------------------|
| Amber (A) | 5 | |
| Blue (Bl) | 6 | |
| Brown (Br) | 5 | |
| Green (G) | 3 | |
| Hazel (H) | 4 | |
| Silver (S) | 1 | |
| TOTAL: | 24 | |

The **frequency** entails from counting the # data points of a given category.

Then compute the total frequency.

Frequency Tables

Given a sample of eye colors:

H, Br, Br, Br, S, A, H, H, G, A, Bl, Bl, Br, Bl, A, Br, H, G, A, A, Br, Bl, G, Bl, Bl

Then the resulting frequency table is:

| EYE COLOR | FREQUENCY | RELATIVE FREQUENCY |
|---------------|-----------|----------------------|
| Amber (A) | 5 | $5/24 \approx 0.208$ |
| Blue (Bl) | 6 | $6/24 = 0.250$ |
| Brown (Br) | 5 | $5/24 \approx 0.208$ |
| Green (G) | 3 | $3/24 = 0.125$ |
| Hazel (H) | 4 | $4/24 \approx 0.167$ |
| Silver (S) | 1 | $1/24 \approx 0.042$ |
| TOTAL: | 24 | 1.000 |

Each category's **relative frequency** is its frequency divided by the total freq. Round decimals to three decimal places as necessary.

The total relative frequency should be very close to one (btw 0.998 & 1.002)

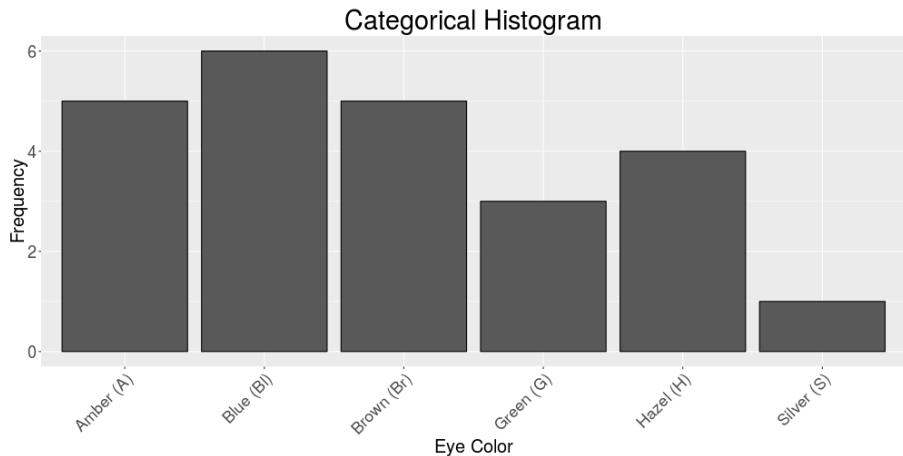
Frequency tables can also be made for numerical data (see the 1.2 Outline).

Histograms for Categorical Data

Given a sample of eye colors:

Br, G, Br, Br, S, A, H, H, G, A, Bl, Bl, Br, Bl, A, Br, H, G, A, A, Br, Bl, G, Bl, Bl

Then the resulting histogram is:

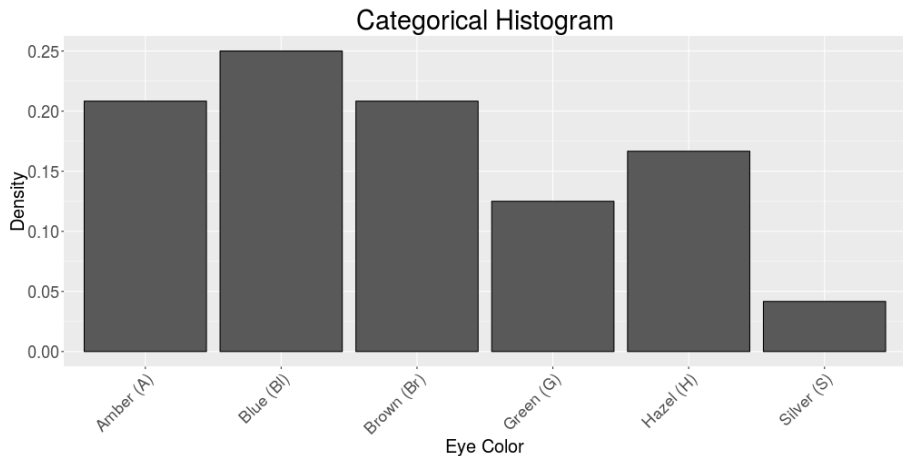


Histograms for Categorical Data

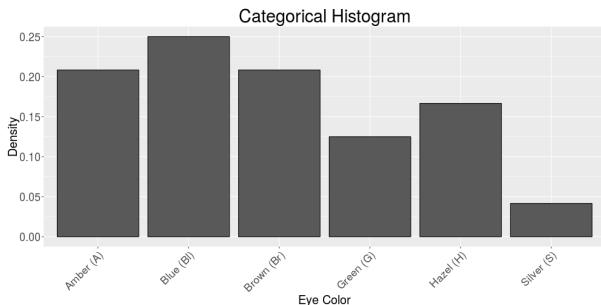
Given a sample of eye colors:

Br, G, Br, Br, S, A, H, H, G, A, Bl, Bl, Br, Bl, A, Br, H, G, A, A, Br, Bl, G, Bl, Bl

Then the resulting histogram is:



Histograms for Categorical Data



The vertical axis of a histogram is always one of the following:

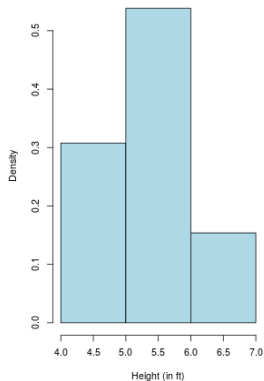
- Frequency (count of each category/bin)
- Relative Frequency = $(\text{Frequency}) / (\text{Total Frequency})$
- Percent (%) = Relative Frequency $\times 100\%$
- Density
 - Categorical Data: Density = Relative Frequency
 - Numerical Data: Density = $(\text{Relative Frequency}) / (\text{Bin Width})$

Histograms for Discrete Data (Equal Bin Widths)

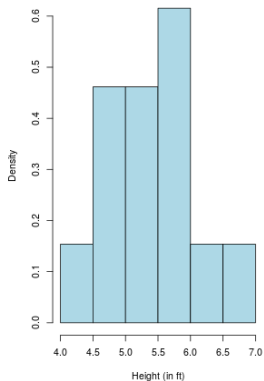
Given a sample: 4.9, 4.9, 5.0, 5.7, 6.2, 5.3, 5.2, 5.5, 5.6, 5.7, 5.7, 4.1, 6.8

Here are three histograms using equal bin widths:

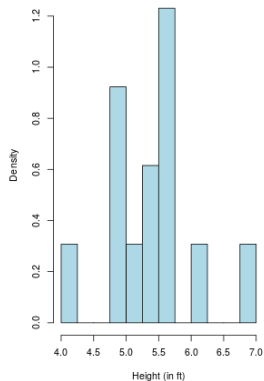
Histogram of Sample (bin width = 1.0 ft)



Histogram of Sample (bin width = 0.50 ft)



Histogram of Sample (bin width = 0.25 ft)

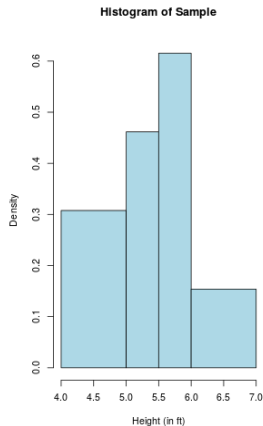
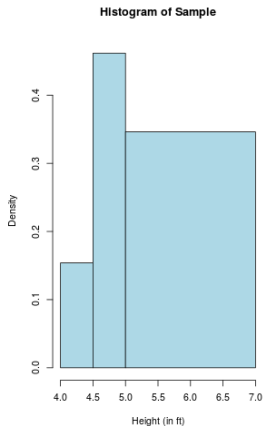
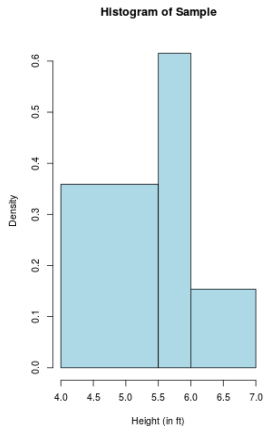


Pick a bin width that avoids gaps (right figure) and "overlumping" (left figure).
For this course, bin widths will be chosen a priori.

Histograms for Discrete Data (Unequal Bin Widths)

Given a sample: 4.9, 4.9, 5.0, 5.7, 6.2, 5.3, 5.2, 5.5, 5.6, 5.7, 5.7, 4.1, 6.8

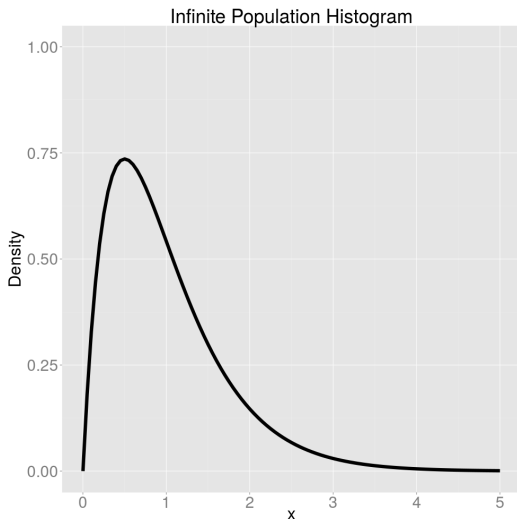
Here are three histograms using unequal bin widths:



Unequal bin widths are useful when there are some isolated data points.
For this course, bin widths will be chosen a priori.

Histograms for Continuous Numerical Data

Continuous numerical data usually refer to infinite populations.
A histogram for an infinite population looks like a smooth curve:



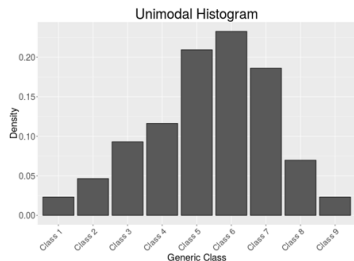
Modality of Discrete & Categorical Data

Definition

A dataset is **unimodal** if its histogram has exactly one peak.

A dataset is **bimodal** if its histogram has exactly two peaks.

A dataset is **multimodal** if its histogram has many peaks.



See page 22 of the textbook for an example of **multimodal** discrete data.

Modality of Continuous Data

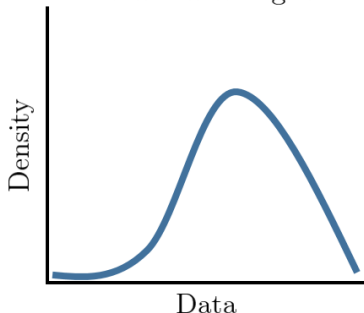
Definition

A dataset is **unimodal** if its histogram has exactly one peak.

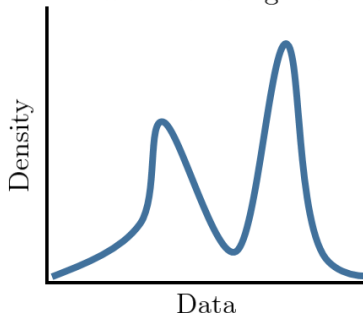
A dataset is **bimodal** if its histogram has exactly two peaks.

A dataset is **multimodal** if its histogram has many peaks.

Unimodal Histogram



Bimodal Histogram



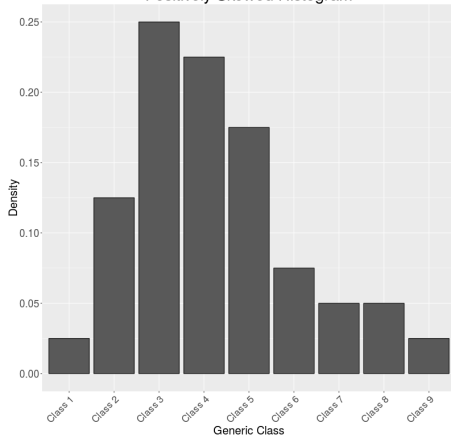
See page 23 of the textbook for an example of **multimodal** continuous data.

Skewness of Discrete & Categorical Data

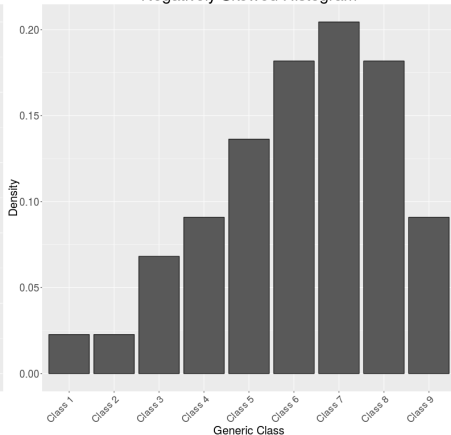
Definition

A dataset is **positively skewed** if its histogram has a long upper tail.
A dataset is **negatively skewed** if its histogram has a long lower tail.

Positively Skewed Histogram



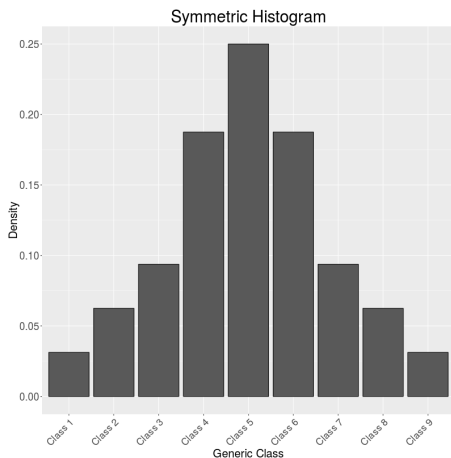
Negatively Skewed Histogram



Skewness of Discrete & Categorical Data

Definition

A dataset is **symmetric** if its histogram's left half and right half are mirror images of each other.

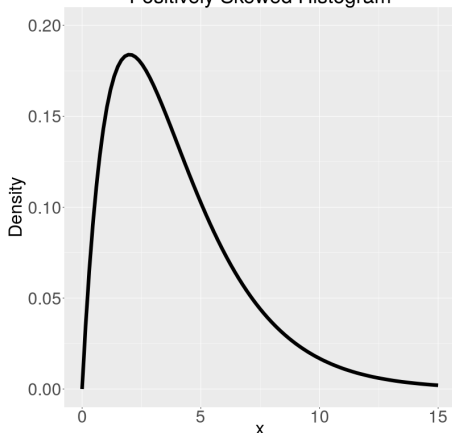


Skewness of Continuous Data

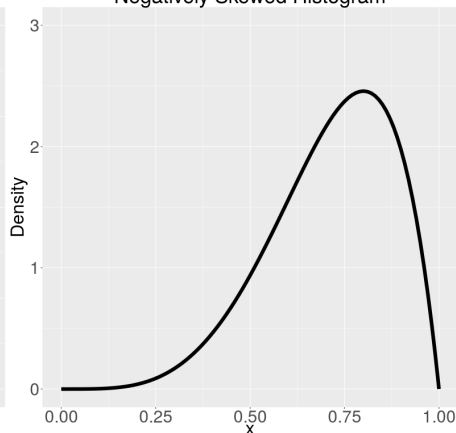
Definition

A dataset is **positively skewed** if its histogram has a long upper tail.
A dataset is **negatively skewed** if its histogram has a long lower tail.

Positively Skewed Histogram



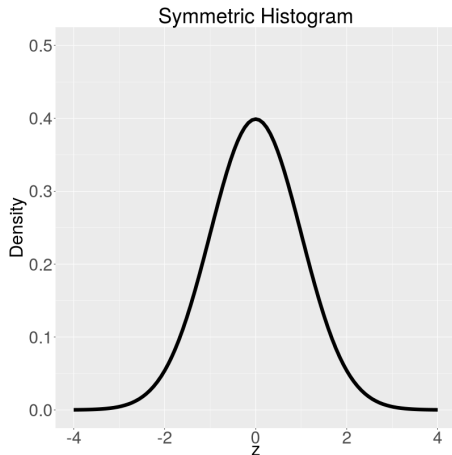
Negatively Skewed Histogram



Skewness of Continuous Data

Definition

A dataset is **symmetric** if its histogram's left half and right half are mirror images of each other.

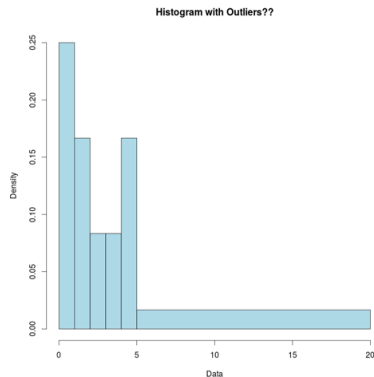
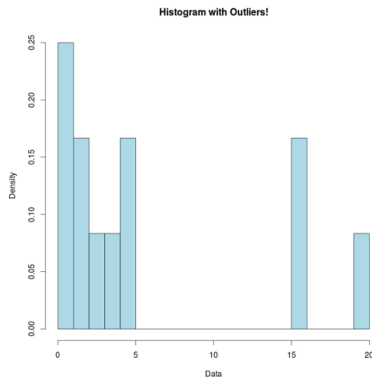


Outlier(s) in Discrete & Categorical Data

Definition

A data point in a dataset is an **outlier** if it is "far away" from "most" of the data.

Consider the dataset: 1,5,2,2,1,4,1,3,20,5,16,16



The left histogram (with equal bin widths) suggest that 16 & 20 are outliers. But identifying outliers is unclear with the right histogram (unequal bin widths).

Outlier(s) in Discrete & Categorical Data

Definition

A data point in a dataset is an **outlier** if it is "far away" from "most" of the data.

- Outliers are essentially extreme values of a dataset or sample.
- Outliers often occur due to catastrophic measurement errors:
 - Instrumentation terribly mis-calibrated
 - Instrumentation malfunctions during measurement
 - Person deliberately lying in a survey
 - Person deliberately exaggerating measurements or counts
- However, not all outliers are due to errors:
 - House prices
 - Exam scores
- Histograms are not always effective in revealing outliers.
- Better visual and numerical methods for identifying outliers in Section 1.4
- Outliers are never really considered for continuous data.

Textbook Logistics for Section 1.2

- Difference(s) in Terminology:

| TEXTBOOK TERMINOLOGY | SLIDES/OUTLINE TERMINOLOGY |
|-----------------------------|-----------------------------------|
| Frequency Distribution | Frequency Table |
| Rectangle Height | Bin Height |
| Class(es) | Bin(s) |
| Class Interval(s) | Bin(s) |
| Class Width | Bin Width |

- Difference(s) in Notation:

| CONCEPT | TEXTBOOK NOTATION | SLIDES/OUTLINE NOTATION |
|----------------|--------------------------|--------------------------------|
| Bin Widths | $3.0 - < 3.5$ | $[3.0, 3.5)$ |

Textbook Logistics for Section 1.2

- Ignore "Stem-and-Leaf Displays" section (pg 13-15)
 - Stem-and-leaf displays were popular prior to the 1980's.
 - Stem-and-leaf displays were useful when computers were text-only.
 - Stem-and-leaf displays will never be used in this course.
- Ignore "Dotplots" section (pg 15-16)
 - Dotplots are effectively histograms but with stacked dots instead of bars.
 - Unfortunately, there's no freedom in choosing appropriate bin widths.
 - Dotplots are only useful for small samples.
 - Dotplots will never be used in this course.
- Ignore "Multivariate Data" section (pg 24)
 - Multivariate Data can be hard or impossible to visualize
 - Multivariate data is never considered in this course.

Fin.