

PRACTICE EXAM 2 - SOLUTIONS (Sections 10.1,10.2,10.4,10.5 & Regression)

* For most problems, only the answer and maybe a hint is given – you have to fill in the details!

* Exception to the above : Problem 1 is solved merely by visual inspection of the given graph

1. a) h increases over interval $(a, b) \cup (d, e) \cup (p, r)$ b) h decreases over $(b, d) \cup (e, p) \cup (r, s)$
 c) Relative minima : $x \in \{d, p\}$ Relative maxima : $x \in \{b, e, r\}$
 d) h is concave up over $(c, e) \cup (e, q)$ e) h is concave down over $(a, c) \cup (q, s)$
 f) Inflection points : $x \in \{c, q\}$
 g) Absolute minimum occurs at $x = s$ h) Absolute maximum occurs at $x = e$
2. a) Acceptable answers: $(-\infty, 0) \cup (0, \infty)$ or $(-\infty, \infty)$ or \mathbb{R} or “All real numbers”
 b) Acceptable answers: \emptyset or “Nowhere” or “No real numbers” c) None
 d) $(-\infty, 0)$ e) $(0, \infty)$ f) $x = 0$
3. a) Acceptable answers: $(-\infty, 1) \cup (1, \infty)$ or $\mathbb{R} \setminus \{1\}$ or “All real numbers except 1”
 b) Acceptable answers: \emptyset or “Nowhere” or “No real numbers” c) None
 d) $(1, \infty)$ e) $(-\infty, 1)$ f) Acceptable answers: $x = 1$ or the point $(1, 3)$
 g) Absolute minimum occurs at $x = -3$ with absolute minimum value of $g(-3) = -125$
 Absolute maximum occurs at $x = 3$ with absolute maximum value of $g(3) = 19$
4. a) $P'(x) = -2x + 8$ b) The monthly advertising budget should be 4000 dollars per month.
5. Length = 12.5 ft and Width = 10 ft, which implies the maximum area of the garden is 125 ft².
6. L = 6.846 ft and W = 8.680 ft, which implies the least amount of fencing used is 58.433 ft
 [all values rounded to 3 decimal places]
7. $y = 0.9303x + 0.4549$ with $R^2 = 0.5617$

BONUS QUESTIONS:

- (B1) $y = -0.3483x^3 + 2.3977x^2 - 3.7119x + 2.6141$ with $R^2 = 0.6370$
 (B2) $y = 0.7714(1.5468^x)$ with $R^2 = 0.4614$
 (B3) Cubic model is the best-fit because its R^2 -value is the closest to 1.
 (B4) ??? (come by my office hours and tell me what your answer is)