

# Regression Model Features

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## Regression Model Features

STAT CALC menu items **3** through **C** are regression models (page 12-24). The automatic residual list and automatic regression equation features apply to all regression models. Diagnostics display mode applies to some regression models.

## Automatic Residual List

When you execute a regression model, the automatic residual list feature computes and stores the residuals to the list name **RESID**. **RESID** becomes an item on the LIST NAMES menu (Chapter 11).

```

NAME OPS MATH
1:ABC
2:RESID
  
```

The TI-82 STATS uses the formula below to compute **RESID** list elements. The next section describes the variable **RegEQ**.

$$\text{RESID} = Ylistname - \text{RegEQ}(Xlistname)$$

## Automatic Regression Equation

Each regression model has an optional argument, *regequ*, for which you can specify a Y= variable such as **Y1**. Upon execution, the regression equation is stored automatically to the specified Y= variable and the Y= function is selected.

```

(1,2,3)→L1:(-1,-
2,-5)→L2
      (-1 -2 -5)
LinReg(ax+b) L1,
L2,Y3
  
```

```

LinReg
y=ax+b
a=-2
b=1.333333333
  
```

```

Plot1 Y1 Plot3
\Y1=
\Y2=
\Y3=-2X+1.333333
3333333
  
```

Regardless of whether you specify a Y= variable for *regequ*, the regression equation always is stored to the TI-82 STATS variable **RegEQ**, which is item **1** on the VARS Statistics EQ secondary menu.

```

XY Σ EQ TEST PTS
1:RegEQ
2:a
3:b
  
```

**Note:** For the regression equation, you can use the fixed-decimal mode setting to control the number of digits stored after the decimal point (Chapter 1). However, limiting the number of digits to a small number could affect the accuracy of the fit.

## Diagnostics Display Mode

When you execute some regression models, the TI-82 STATS computes and stores diagnostics values for  $r$  (correlation coefficient) and  $r^2$  (coefficient of determination) or for  $R^2$  (coefficient of determination).

$r$  and  $r^2$  are computed and stored for these regression models.

<b>LinReg(ax+b)</b>	<b>LnReg</b>	<b>PwrReg</b>
<b>LinReg(a+bx)</b>	<b>ExpReg</b>	

$R^2$  is computed and stored for these regression models.

<b>QuadReg</b>	<b>CubicReg</b>	<b>QuartReg</b>
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The  $r$  and  $r^2$  that are computed for **LnReg**, **ExpReg**, and **PwrReg** are based on the linearly transformed data. For example, for **ExpReg** ( $y=ab^x$ ),  $r$  and  $r^2$  are computed on  $\ln y = \ln a + x(\ln b)$ .

By default, these values are not displayed with the results of a regression model when you execute it. However, you can set the diagnostics display mode by executing the **DiagnosticOn** or **DiagnosticOff** instruction. Each instruction is in the CATALOG (Chapter 15).

```

CATALOG
det(
DiagnosticOff
DiagnosticOn
dim(
  
```

**Note:** To set **DiagnosticOn** or **DiagnosticOff** from the home screen, press **2nd** [CATALOG], and then select the instruction for the mode you want. The instruction is pasted to the home screen. Press **ENTER** to set the mode.

When **DiagnosticOn** is set, diagnostics are displayed with the results when you execute a regression model.

```

DiagnosticOn
Done
LinReg(ax+b) L1,
L2
  
```

```

LinReg
y=ax+b
a=-2
b=1.333333333
r^2=.9230769231
r=-.9607689228
  
```

When **DiagnosticOff** is set, diagnostics are not displayed with the results when you execute a regression model.

```

DiagnosticOff
Done
LinReg(ax+b) L1,
L2
  
```

```

LinReg
y=ax+b
a=-2
b=1.333333333
  
```

# STAT CALC Menu

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## STAT CALC Menu

To display the STAT CALC menu, press  $\boxed{\text{STAT}}$   $\boxed{\blacktriangleright}$ .

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### EDIT **CALC** TESTS

<b>1:</b> 1-Var Stats	Calculates 1-variable statistics.
<b>2:</b> 2-Var Stats	Calculates 2-variable statistics.
<b>3:</b> Med-Med	Calculates a median-median line.
<b>4:</b> LinReg(ax+b)	Fits a linear model to data.
<b>5:</b> QuadReg	Fits a quadratic model to data.
<b>6:</b> CubicReg	Fits a cubic model to data.
<b>7:</b> QuartReg	Fits a quartic model to data.
<b>8:</b> LinReg(a+bx)	Fits a linear model to data.
<b>9:</b> LnReg	Fits a logarithmic model to data.
<b>0:</b> ExpReg	Fits an exponential model to data.
<b>A:</b> PwrReg	Fits a power model to data.
<b>B:</b> Logistic	Fits a logistic model to data.
<b>C:</b> SinReg	Fits a sinusoidal model to data.

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For each STAT CALC menu item, if neither *Xlistname* nor *Ylistname* is specified, then the default list names are **L1** and **L2**. If you do not specify *freqlist*, then the default is **1** occurrence of each list element.

## Frequency of Occurrence for Data Points

For most STAT CALC menu items, you can specify a list of data occurrences, or frequencies (*freqlist*).

Each element in *freqlist* indicates how many times the corresponding data point or data pair occurs in the data set you are analyzing.

For example, if **L1**={15,12,9,14} and **LFREQ**={1,4,1,3}, then the TI-82 STATS interprets the instruction **1-Var Stats L1, LFREQ** to mean that **15** occurs once, **12** occurs four times, **9** occurs once, and **14** occurs three times.

Each element in *freqlist* must be  $\geq 0$ , and at least one element must be  $> 0$ .

Noninteger *freqlist* elements are valid. This is useful when entering frequencies expressed as percentages or parts that add up to 1. However, if *freqlist* contains noninteger frequencies, **Sx** and **Sy** are undefined; values are not displayed for **Sx** and **Sy** in the statistical results.

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## 1-Var Stats

**1-Var Stats** (one-variable statistics) analyzes data with one measured variable. Each element in *freqlist* is the frequency of occurrence for each corresponding data point in *Xlistname*. *freqlist* elements must be real numbers  $> 0$ .

**1-Var Stats** [*Xlistname*,*freqlist*]

```
1-Var Stats L1,L2
■
```

## 2-Var Stats

**2-Var Stats** (two-variable statistics) analyzes paired data. *Xlistname* is the independent variable. *Ylistname* is the dependent variable. Each element in *freqlist* is the frequency of occurrence for each data pair (*Xlistname*,*Ylistname*).

**2-Var Stats** [*Xlistname*,*Ylistname*,*freqlist*]

## Med-Med (ax+b)

**Med-Med** (median-median) fits the model equation  $y=ax+b$  to the data using the median-median line (resistant line) technique, calculating the summary points **x1**, **y1**, **x2**, **y2**, **x3**, and **y3**. **Med-Med** displays values for **a** (slope) and **b** (y-intercept).

**Med-Med** [*Xlistname*,*Ylistname*,*freqlist*,*regequ*]

```
Med-Med L3,L4,Y2
■
```

```
Med-Med
y=ax+b
a=.875
b=1.541666667
```

## LinReg (ax+b)

**LinReg(ax+b)** (linear regression) fits the model equation  $y=ax+b$  to the data using a least-squares fit. It displays values for **a** (slope) and **b** (y-intercept); when **DiagnosticOn** is set, it also displays values for  $r^2$  and **r**.

**LinReg(ax+b)** [*Xlistname*,*Ylistname*,*freqlist*,*regequ*]

## QuadReg (ax<sup>2</sup>+bx+c)

**QuadReg** (quadratic regression) fits the second-degree polynomial  $y=ax^2+bx+c$  to the data. It displays values for **a**, **b**, and **c**; when **DiagnosticOn** is set, it also displays a value for **R<sup>2</sup>**. For three data points, the equation is a polynomial fit; for four or more, it is a polynomial regression. At least three data points are required.

**QuadReg** [*Xlistname*,*Ylistname*,*freqlist*,*regequ*]

## STAT CALC Menu (continued)

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**CubicReg**  
**( $ax^3+bx^2+cx+d$ )**

**CubicReg** (cubic regression) fits the third-degree polynomial  $y=ax^3+bx^2+cx+d$  to the data. It displays values for **a**, **b**, **c**, and **d**; when **DiagnosticOn** is set, it also displays a value for **R<sup>2</sup>**. For four points, the equation is a polynomial fit; for five or more, it is a polynomial regression. At least four points are required.

**CubicReg** [*Xlistname*,*Ylistname*,*freqlist*,*regequ*]

**QuartReg**  
**( $ax^4+bx^3+cx^2+dx+e$ )**

**QuartReg** (quartic regression) fits the fourth-degree polynomial  $y=ax^4+bx^3+cx^2+dx+e$  to the data. It displays values for **a**, **b**, **c**, **d**, and **e**; when **DiagnosticOn** is set, it also displays a value for **R<sup>2</sup>**. For five points, the equation is a polynomial fit; for six or more, it is a polynomial regression. At least five points are required.

**QuartReg** [*Xlistname*,*Ylistname*,*freqlist*,*regequ*]

**LinReg**  
**( $a+bx$ )**

**LinReg( $a+bx$ )** (linear regression) fits the model equation  $y=a+bx$  to the data using a least-squares fit. It displays values for **a** (y-intercept) and **b** (slope); when **DiagnosticOn** is set, it also displays values for **r<sup>2</sup>** and **r**.

**LinReg( $a+bx$ )** [*Xlistname*,*Ylistname*,*freqlist*,*regequ*]

**LnReg**  
**( $a+b \ln(x)$ )**

**LnReg** (logarithmic regression) fits the model equation  $y=a+b \ln(x)$  to the data using a least-squares fit and transformed values  $\ln(x)$  and  $y$ . It displays values for **a** and **b**; when **DiagnosticOn** is set, it also displays values for **r<sup>2</sup>** and **r**.

**LnReg** [*Xlistname*,*Ylistname*,*freqlist*,*regequ*]

**ExpReg**  
**( $ab^x$ )**

**ExpReg** (exponential regression) fits the model equation  $y=ab^x$  to the data using a least-squares fit and transformed values  $x$  and  $\ln(y)$ . It displays values for **a** and **b**; when **DiagnosticOn** is set, it also displays values for **r<sup>2</sup>** and **r**.

**ExpReg** [*Xlistname*,*Ylistname*,*freqlist*,*regequ*]

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**PwrReg**  
**(ax<sup>b</sup>)**

**PwrReg** (power regression) fits the model equation  $y=ax^b$  to the data using a least-squares fit and transformed values  $\ln(x)$  and  $\ln(y)$ . It displays values for **a** and **b**; when **DiagnosticOn** is set, it also displays values for **r<sup>2</sup>** and **r**.

**PwrReg** [*Xlistname*,*Ylistname*,*freqlist*,*regequ*]

**Logistic**  
**c/(1+a\*e<sup>-bx</sup>)**

**Logistic** fits the model equation  $y=c/(1+a*e^{-bx})$  to the data using an iterative least-squares fit. It displays values for **a**, **b**, and **c**.

**Logistic** [*Xlistname*,*Ylistname*,*freqlist*,*regequ*]

**SinReg**  
**a sin(bx+c)+d**

**SinReg** (sinusoidal regression) fits the model equation  $y=a \sin(bx+c)+d$  to the data using an iterative least-squares fit. It displays values for **a**, **b**, **c**, and **d**. At least four data points are required. At least two data points per cycle are required in order to avoid aliased frequency estimates.

**SinReg** [*iterations*,*Xlistname*,*Ylistname*,*period*,*regequ*]

*iterations* is the maximum number of times the algorithm will iterate to find a solution. The value for *iterations* can be an integer  $\geq 1$  and  $\leq 16$ ; if not specified, the default is 3. The algorithm may find a solution before *iterations* is reached. Typically, larger values for *iterations* result in longer execution times and better accuracy for **SinReg**, and vice versa.

A *period* guess is optional. If you do not specify *period*, the difference between time values in *Xlistname* must be equal and the time values must be ordered in ascending sequential order. If you specify *period*, the algorithm may find a solution more quickly, or it may find a solution when it would not have found one if you had omitted a value for *period*. If you specify *period*, the differences between time values in *Xlistname* can be unequal.

**Note:** The output of **SinReg** is always in radians, regardless of the **Radian/Degree** mode setting.

A **SinReg** example is shown on the next page.

# STAT CALC Menu (continued)

## SinReg Example: Daylight Hours in Alaska for One Year

Compute the regression model for the number of hours of daylight in Alaska during one year.

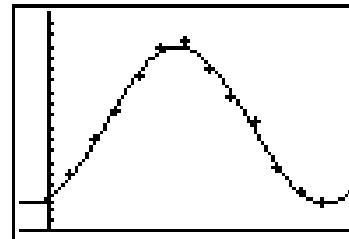
```
seq(X,X,1,361,30
)→L1:(5.5,8,11,1
3.5,16.5,19,19.5
,17,14.5,12.5,8.
5,6.5,5.5)→L2
(5.5 8 11 13.5 ...
```



```
21021 Plot2 Plot3
Off Off
Type: [ ] [ ] [ ]
[ ] [ ] [ ]
Xlist:L1
Ylist:L2
Mark: [ ] [ ] [ ]
```

```
SinReg L1,L2,Y1
```

```
SinReg
y=a*sin(bx+c)+d
a=6.770292445
b=.0162697853
c=-1.215498579
d=12.18138372
```



← 1 period →

With noisy data, you will achieve better convergence results when you specify an accurate estimate for *period*. You can obtain a *period* guess in either of two ways.

- Plot the data and trace to determine the x-distance between the beginning and end of one complete period, or cycle. The illustration above and to the right graphically depicts a complete period, or cycle.
- Plot the data and trace to determine the x-distance between the beginning and end of N complete periods, or cycles. Then divide the total distance by N.

After your first attempt to use **SinReg** and the default value for *iterations* to fit the data, you may find the fit to be approximately correct, but not optimal. For an optimal fit, execute **SinReg 16,Xlistname,Ylistname,2π / b** where *b* is the value obtained from the previous **SinReg** execution.